

# Dynamics in $(r, \varphi, \Upsilon)$ in $(i, j, k)$

- solution for the relative motion:  $\mathbf{r} = r \cos \varphi \mathbf{i} + r \sin \varphi \mathbf{j}$

- the basic vectors: 
$$\begin{pmatrix} \mathbf{i} \\ \mathbf{j} \\ \mathbf{k} \end{pmatrix} = \mathcal{R}(i, \Theta) \mathcal{R}(e_Z, \Upsilon) \begin{pmatrix} \mathbf{e}_X \\ \mathbf{e}_Y \\ \mathbf{e}_Z \end{pmatrix}$$

- the quasi-Keplerian representation:

$$r = a_r(1 - e_r \cos u), \quad n(t - t_0) = u - e_t \sin u,$$

$$\varphi - \varphi_0 = (1 + k)v,$$

$$\Upsilon - \Upsilon_0 = \frac{\chi_{\text{so}} J}{c^2 L^3} (v + e \sin v),$$

$$v = 2 \arctan \left[ \left( \frac{1 + e_\varphi}{1 - e_\varphi} \right)^{1/2} \tan \frac{u}{2} \right]$$