

3PN Binary BH Conservative Dynamics

$$\begin{aligned} H(t) &= m_1 c^2 + m_2 c^2 + H_N + \frac{1}{c^2} H_{[1PN]} \\ &+ \frac{1}{c^4} H_{[2PN]} + \frac{1}{c^6} H_{[3PN]} + \dots \\ &+ \frac{1}{c^5} H_{[2.5PN]}(t) + \frac{1}{c^7} H_{[3.5PN]}(t) + \dots \end{aligned}$$

$$\hat{H} = (H - Mc^2)/\mu, \quad \mu = m_1 m_2 / M, \quad M = m_1 + m_2$$

$$\nu = \mu/M, \quad 0 \leq \nu \leq 1/4$$

test-body case: $\nu = 0$, equal-mass case: $\nu = 1/4$

CMS: $\mathbf{p}_1 + \mathbf{p}_2 = 0$, $\mathbf{p} \equiv \mathbf{p}_1/\mu$,

$p_r = (\mathbf{n} \cdot \mathbf{p})$, $\mathbf{q} \equiv (\mathbf{x}_1 - \mathbf{x}_2)/GM$, $\mathbf{n} = \mathbf{q}/|\mathbf{q}|$